

# Robust Epsilon Visibility

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<http://www-sop.inria.fr/revs>



## Overview

- Introduction
- Previous Work
- Generalized Visibility Events
- Enumeration and Validation
- Robust Blocker Predicates
- Implementation and Results
- Conclusion



## Introduction

- Analytic visibility algorithms
  - continuous & precise solution, but not robust



[Durand et al. 99]

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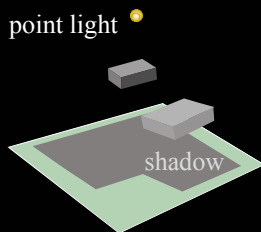


## Analytic Visibility is Not Robust

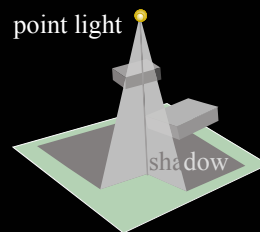
- Geometric complexity and degeneracies
  - touching objects
  - coplanar edges (e.g., chairs in a concert hall)
  - aligned vertices
  - floating point arithmetic can't handle small features: geometric algorithms fail



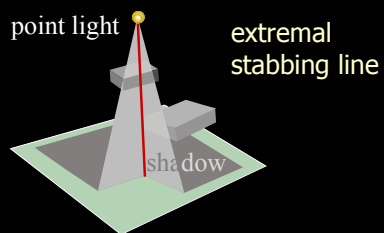
## Introduction: Shadow Boundaries



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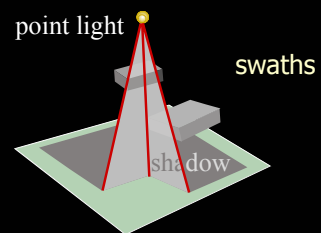
## Introduction: Shadow Boundaries



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## Introduction: Shadow Boundaries

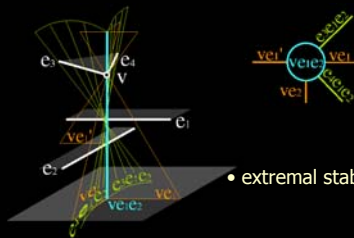


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## Introduction: Visibility Skeleton

- Visibility Skeleton [Durand et al. '97]



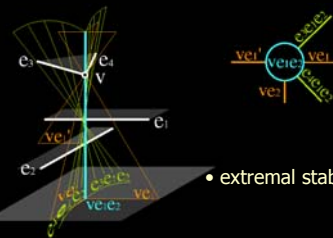
- extremal stabbing line  $ve_1e_2$

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## Introduction: Visibility Skeleton

- Visibility Skeleton [Durand et al. '97]



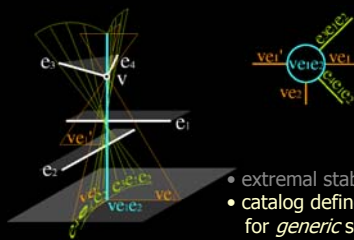
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## Introduction: Visibility Skeleton

- Visibility Skeleton [Durand et al. '97]



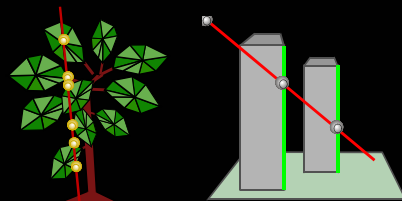
- extremal stabbing line  $ve_1e_2$
- catalog defines adjacencies for *generic* scenes

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## Need to Treat Degeneracies

- Real scenes are degenerate !
- Catalog will fail



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## Our Solution

- Generalize the idea of extremal stabbing line (ESL)
- Develop a robust ESL casting process
- Robust swath construction
- Robust blocker predicates



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## Previous Work

- Analytic visibility
  - aspect graph [Koenderink '79]
- Analytic visibility in graphics
  - extremal stabbing lines, and swaths [Teller '92]



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## Previous Work

- Discontinuity Meshes
  - [Heckbert '91, '92], [Lischinski et al. '92]
  - complete DM [Drettakis & Fiume '94], [Stewart & Ghali '94]
- Visibility Complex and Visibility Skeleton
  - [Durand et al. '96, '97]



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## Previous Work

- Epsilon geometry
  - imprecise calculations [Salesin et al. '89]
- Interval methods
  - implicit functions etc. [Snyder '92]
  - ray tracing [Bala et al. '99]



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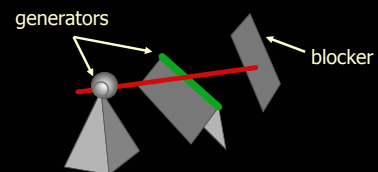


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## Generalized Visibility Events

- Basic definitions
  - generator: edge or vertex of the scene
  - blocker: any geometric element

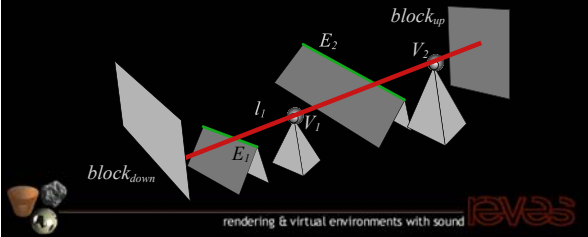


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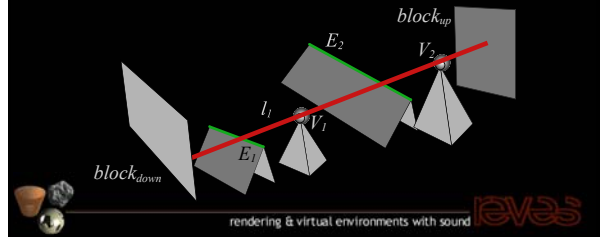
## Generalized Visibility Events

- Extremal Stabbing Line (ESL):
  - quadri-tangent (VV, VEE, E4)
  - data structure containing generators



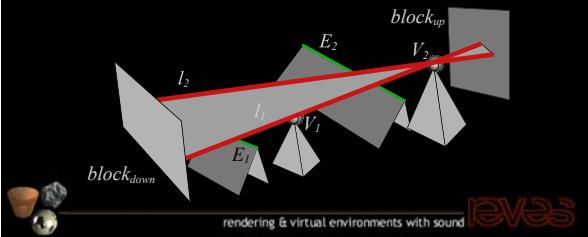
## Generalized Visibility Events

- General Extremal Stabbing Line
  - catalog will fail



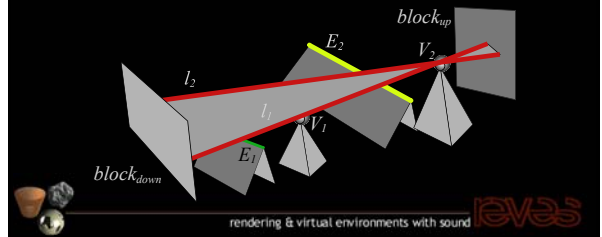
## Generalized Visibility Events

- Critical Line Swath
  - connects extremal stabbing lines
  - defined procedurally



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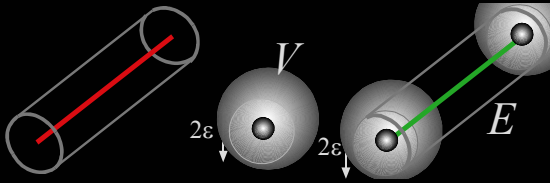


## Enumeration and Validation

- On demand computation for an emitter/receiver pair
  - equivalent to lazy evaluation of Visibility Skeleton
- Methodology to enumerate & validate ESL's and swaths
  - propose ESL's (VV, VEE, E4)
  - occlusion computations: ESL casting
    - treatment of degeneracies
  - join ESL's with swaths



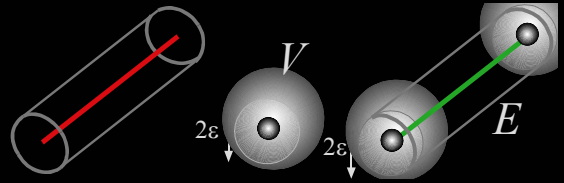
## Fat Elements



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## Fat Elements



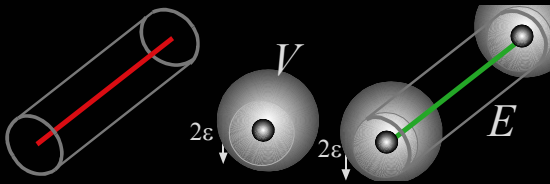
fat line



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## Fat Elements



fat line

fat elements



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## ESL Casting Algorithm

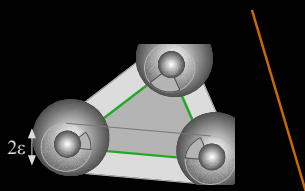
- $\varepsilon$  methods or predicates for ESL-face interactions
- local occlusion test
- casting process



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## ESL-face Interaction



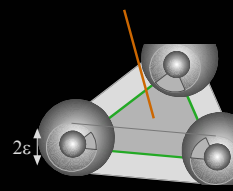
no stab



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## ESL-face Interaction



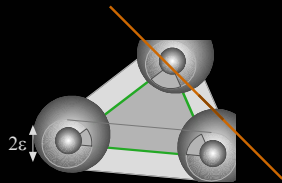
full stab



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## ESL-face Interaction



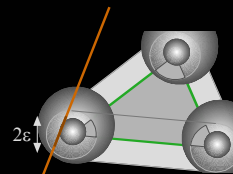
edge stab



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## ESL-face Interaction



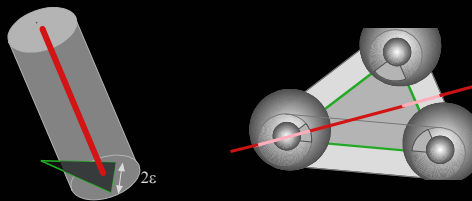
vertex stab



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## ESL-face Interaction



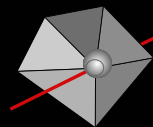
multi stab



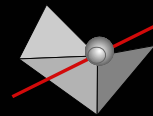
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## Local Occlusion Test



■ blocker



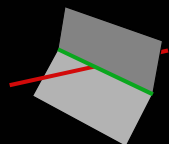
■ generator



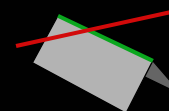
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## Local Occlusion Test



■ blocker



■ generator



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## ESL Casting

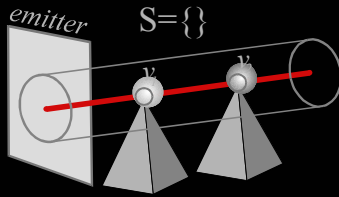
- ESL candidate with *native* generators
  - VV, VEE, E4
- S initially an empty set
- Algorithm: cast a line in scene
  - for each hit element, blocker/generator ?
    - if generator, insert to S
    - else stop
- ESL valid if all native generators in S



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## ESL Casting

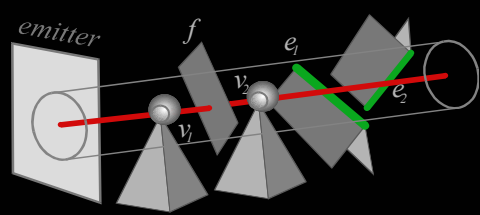


Native VV ESL

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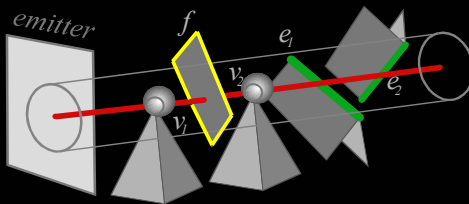
## ESL Casting



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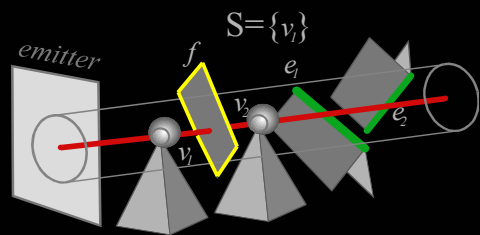
## ESL Casting



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## ESL Casting

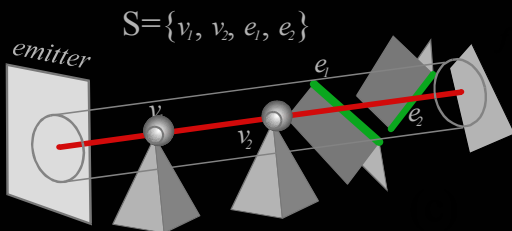


Native generators not included in S: invalid ESL

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## ESL Casting



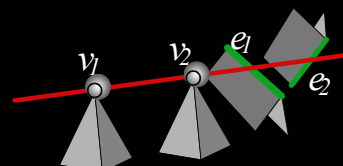
Native generators included in S: valid ESL

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## Redundant ESL's

### Redundant enumerations



- $v_1, v_2$
- $v_1, e_1, e_2$
- $v_2, e_1, e_2$

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## Redundant ESL's

- Two conditions for redundancy:
  - combinatorial condition: are the native generators contained in  $S$ ?
  - topological condition: is the distance smaller than epsilon?
    - distance: within the shaft

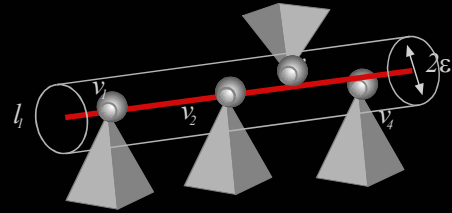
note: test performed **before** casting



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## Redundant ESL's



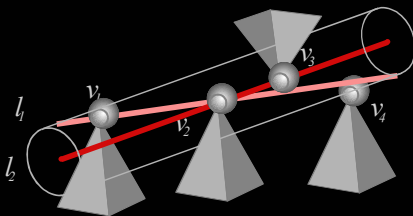
ESL with  $S = \{v_1, v_2, v_3, v_4\}$  where  $v_1, v_2$  native



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## Redundant ESL's



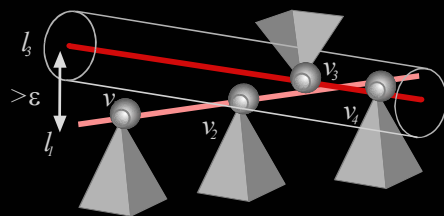
Both criteria are met:  $l_2$  is redundant



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## Redundant ESL's



Combinatorial condition met, but not topological:  $l_3$  is maintained



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## Critical Line Swaths

- Enumeration:
  - loop through VE and EEE
  - shared pair of ESL's?
  - if yes, create candidate swath
- Validation:
  - assumption: all ESL's computed
  - occlusion test
  - midline casting



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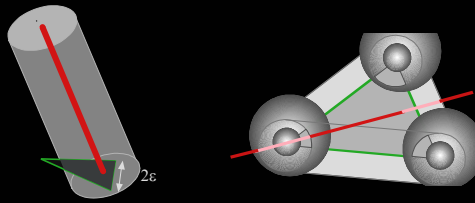


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## ESL-face Interaction



multi stab



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## Robust Blocker Predicates

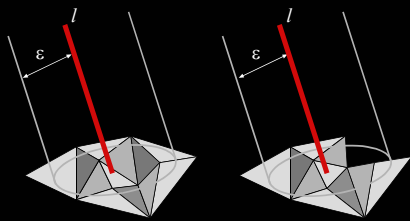
- Multi-face
  - connectivity available
- Blocker-fan
  - connectivity unavailable or touching objects



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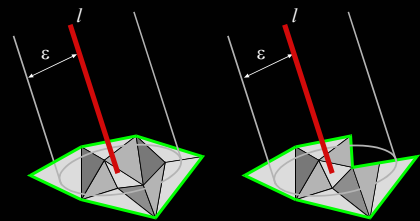
## Multi-face Construction



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## Multi-face Construction



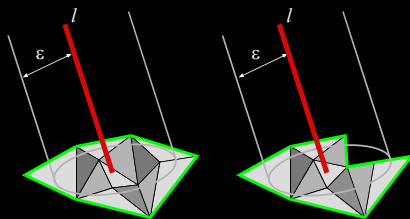
blocked



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## Multi-face Construction



blocked

not blocked



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## Blocker-fan

- Progressive contribution to ray occlusion
  - contacts
  - special-hit configurations
  - identification of the blocker (vertex/edge/face)



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## Blocker-fan

- Based on thick slices: depth component added to regular slices
  - progressively insert thick slices
  - merge slices only if depth overlaps
  - if complete disc, last element is blocker



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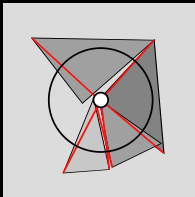
## Blocker-fan



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## Blocker-fan



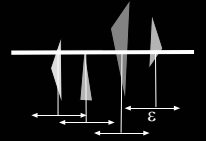
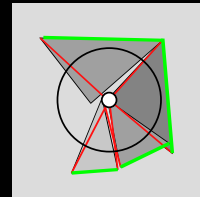
slices do not form a complete disc



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## Blocker-fan



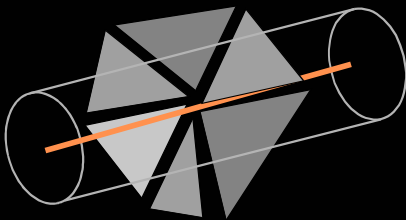
slices do not form a complete disc  
slices do not overlap in depth: not blocked



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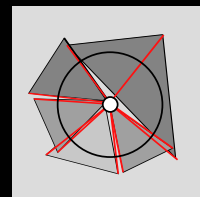
## Blocker-fan



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## Blocker-fan



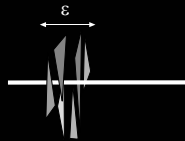
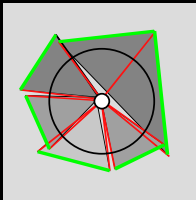
slices form a complete disc



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## Blocker-fan



slices form a complete disc  
slices overlap in depth: blocked



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## Implementation and Results

- Shadow boundary computation
  - Point or Directional Light source
    - equivalent to a 2D problem
    - constrained Delaunay triangulation for lighting
  - Area (polygonal) light source
    - shadow boundaries (discontinuity mesh)
    - problem with CDT



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64,000 input polygons



eps = 0.0001

smesh = 270,000



eps = 0.001

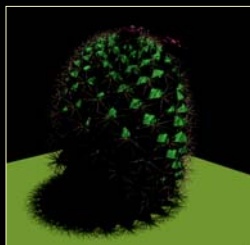
smesh = 220,000



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## Cactus Model



34,000 input polygons



428,000 shadow mesh

1 h 10 min (Pentium III, 1 Ghz)



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## Big Scene



121,000 input polygons



330,000 shadow mesh

10 min (Pentium III, 1 Ghz)



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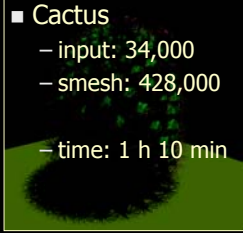
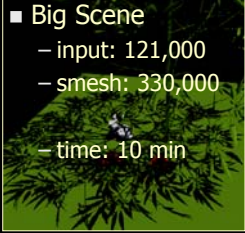
## Big Scene vs Cactus

### ■ Big Scene

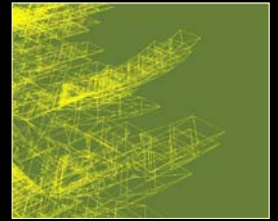
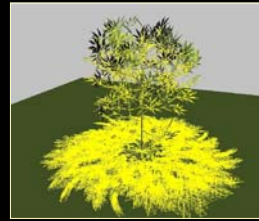
- input: 121,000
- smesh: 330,000
- time: 10 min

### ■ Cactus

- input: 34,000
- smesh: 428,000
- time: 1 h 10 min



## Soft Shadow Boundaries

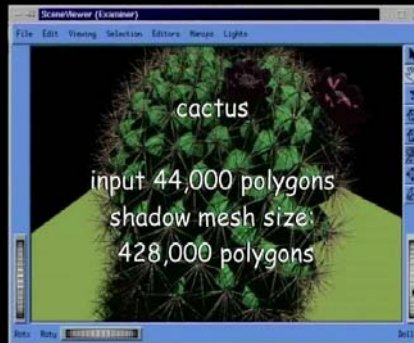


34,000 input polygons

464,000 swaths

17 h 30 min (Pentium III, 1 Ghz) naive algorithm

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## Discussion

- + robust analytic visibility for real scenes
- + consistent feature merging
- computationally expensive
- size of soft shadow mesh

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## Future Work

- lighting for soft shadows
  - simplification of shadow mesh
  - robust CDT
- optimization for soft shadows
  - hierarchies
- general visibility tool
  - global illumination
  - walkthroughs etc.

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## Conclusion

- generalized definition of visibility events
- epsilon visibility methods
- robust ESL casting and swath construction algorithm
- robust blocker predicates
- results on real-world models

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## Acknowledgments

- Frédo Durand for initial ideas and help
- Marc Stamminger and Pierre Poulin
- Ecole Nationale Supérieure des Télécommunications (Paris)
- INRIA National Research Initiative (ARC) "Visi3D" on 3D Visibility



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Thank you

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Thank you

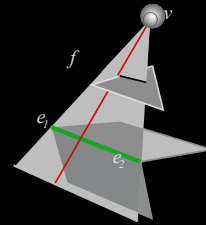
<http://www.sop.inria.fr/reves>



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## Swath validation

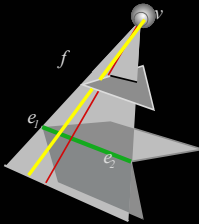


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## Swath validation

- midline not blocked: valid swath

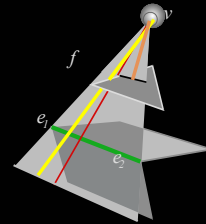


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## Swath validation

- midline blocked: no swath



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## Sharp shadows

- Generators
  - Light source (vertex or equivalent)
  - For ESL candidates:
    - two edges (one silhouette), SEE
    - vertex (connected to a silhouette edge), SV
  - For Swaths
    - edge (silhouette), SE
- Enumeration
  - vertices and edges pairs, with nested ESL casting
  - Swath, with nested Swath validation



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## Soft Shadows

- Light source is a convex planar polygon
- Generators
  - Vertex (Vs) or Edge (Es) of the light source
  - ESL candidates
    - VsV, VsEE
    - EsVE, EsEEE
  - Swath candidates
    - VsE
    - EsV
    - EsEE



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## Generalized Visibility Events

- On demand computations for an emitter/receiver pair
  - equivalent to lazy evaluation of Visibility Skeleton



## Discussion

- Possible cases of failure
  - faut la faire

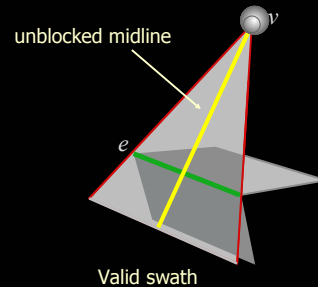


## Enumeration and Validation

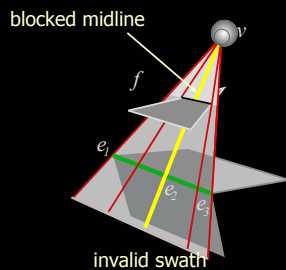
- ESL Casting
  - from an ESL candidate (set of generators, marked as native), test occlusion
- Swath Validation
  - from a swath candidate (set of generators, native), test critical line set and occlusion



## Swath validation



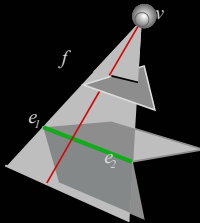
## Swath validation



Thank you



## Swath validation

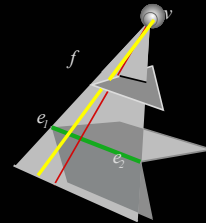


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## Swath validation

- midline not blocked: valid swath

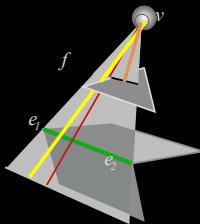


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## Swath validation

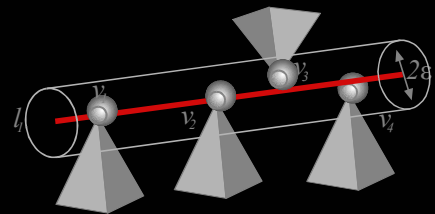
- midline blocked: no swath



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## Redundant ESL's

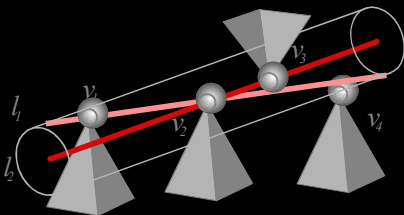


ESL with  $S = \{v_1, v_2, v_3, v_4\}$  where  $v_1, v_2$  native

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## Redundant ESL's



Both criteria are met:  $l_2$  is redundant

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